Chapter 2 Structural Equation Modeling Merle Canfield

The next three computer runs demonstrate the use of multiple regression in decomposing variance.

LSQREG2.SPS
set printer=off. set eject on. set ccho on. set screen=off. set length=59. translate from 'aftrel.dbf/type=db4/ keep = ENIOY FGOOD WORTH FEARFUL ANGRY TENSE SHY SAD BORED FUN WORRIED SORRY OUTGOING COPERTIV SUSPICIS SATISFID CHARM TOUCHED PEOPLE DISAGREE SIXSENSE HCONFLIC ARRANGE INCLUDED GENTLE LIKEME OUTSELF ALONG CONFRONT RESOLVED FRCONFLT FRFEE FRSUPP FRPROD FRLEIS TTALK. MISSING VALUES enjoy to ttalk (9). compute shy=ln(shy). compute bored=ln(bored). compute sory=ln(sory). compute suspicis=ln(suspicis). REGRESSION DESCRIPTIVES=MEAN STDDEV CORR N /variables = fgood worth angry arrange copertiv outgoing /statistics = r coeff anova outs zp cha /DEPENDENT=angry /method=enter outgoing. finish

Notice the two variables of ARRANGE and COPERTIV are forced to enter the equation first (/method=enter ARRANGE COPERTIV) and then the variable OUTGOING is entered (/method=enter OUTGOING). Partial output follows:

Equation Number 1 Dependent Variable.. FGOOD Beginning Block Number 1. Method: Enter ARRANGE COPERTIV

Variable(s) Entered on Step Number

- 1.. COPERTIV
- 2.. ARRANGE

Multiple R .60306

R Square	.36368	R Square Change	.36368
Adjusted R Square	.34985	F Change	26.29122
Standard Error	1.46552	Signif F Change	.0000
Equation Number 1	Dependent Va	ariable FGOOD	
Beginning Block Nu	mber 2. Metho	d: Enter OUTO	GOING
Variable(s) Entered	l on Step Numbe	r	
3 OUTGOIN	G		
Multiple R	.67478		
R Square	.45533	R Square Change	.09164
Adjusted R Square	.43737	F Change	15.31104
Standard Error	1.36331	Signif F Change	.0002

It is the R Square Change of the last step that is of interest. Note that R Square Change was .09 (that means that OUTGOING accounts for 9% of the variance of FGOOD that is not accounted for by ARRANGE and COPERTIV combined). The next jobstream will test the amount of variance that ARRANGE accounts for in FGOOD beyond OUTGOING and COPERTIV.

Part of LSQREG2.SPS revised

REGRESSION

DESCRIPTIVES=MEAN STDDEV CORR N /variables = fgood worth angry arrange copertiv outgoing /statistics = r coeff anova outs zpp cha /DEPENDENT=angry /method=enter outgoing copertiv /method=enter arrange. finish.

equation Number 1 Dependent Variable.. FGOOD Beginning Block Number 1. Method: Enter OUTGOING COPERTIV Variable(s) Entered on Step Number

- 1.. OUTGOING
- 2.. COPERTIV

Multiple R	.64035		
R Square	.41005	R Square Change	.41005
Adjusted R Square	.39722	F Change	31.97260
Standard Error	1.41112	Signif F Change	.0000

Equation Number 1 Dependent Variable.. FGOOD Beginning Block Number 2. Method: Enter ARRANGE Variable(s) Entered on Step Number

3.. ARRANGE

.67478		
.45533	R Square Change	.04528
.43737	F Change	7.56482
1.36331	Signif F Change	.0072
	.45533 .43737	.45533 R Square Change .43737 F Change

Note in the R Square Change of the last step that ARRANGE account for 5% (rounded and converted from .04528) of the variance of FGOOD beyond OUTGOING and COPERTIV. The next partial jobstream computes the amount of variance accounted for by COPERTIV in FGOOD beyond that of OUTGOING and ARRANGE.

Part of LSQREG2.SPS revised
REGRESSION DESCRIPTIVES=MEAN STDDEV CORR N /variables = fgood worth angry arrange copertiv outgoing /statistics = r coeff anova outs zpp cha /DEPENDENT=angry /method=enter outgoing arrange /method=enter copertiv. finish.

Equation Number 1 Dependent Variable.. FGOOD Beginning Block Number 1. Method: Enter OUTGOING ARRANGE Variable(s) Entered on Step Number

1.. OUTGOING

2.. ARRANGE

 Multiple R
 .62595

 R Square
 .39182
 R Square Change
 .39182

 Adjusted R Square
 .37860
 F Change
 29.63507

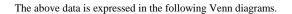
 Standard Error
 1.43276
 Signif F Change
 .0000

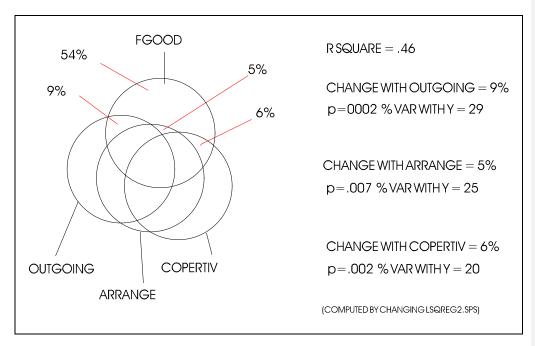
Equation Number 1 Dependent Variable... FGOOD Beginning Block Number 2. Method: Enter COPERTIV Variable(s) Entered on Step Number

3.. COPERTIV

Multiple R	.67478		
R Square	.45533	R Square Change	.06351
Adjusted R Square	.43737	F Change	10.61100
Standard Error	1.36331	Signif F Change	.0016

Note that the R Square Change was .06351 (indicating 6% change) when COPERTIV was entered last. This indicates that COPERTIV accounted for 6% of the variance of FGOOD beyond that of OUTGOING and ARRANGE.





In the next three jobstreams WORTH will be considered as the dependent variable and the same three variables of OUTGOING, ARRANGE, and COPERTIV will once again be treated as independent variables.

Part of LSQREG2.SPS revised

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Comment [COMMENT1]: lsqreg2.cdr

REGRESSION DESCRIPTIVES=MEAN STDDEV CORR N /variables = fgood worth angry arrange copertiv outgoing /statistics = r coeff anova outs zpp cha /DEPENDENT=angry /method=enter arrange copertiv /method=enter outgoing. finish.

Equation Number 1 Dependent Variable.. WORTH Beginning Block Number 1. Method: Enter ARRANGE COPERTIV Variable(s) Entered on Step Number 1.. COPERTIV 2.. ARRANGE Multiple R .48775 R Square .23790 R Square Change .23790 Adjusted R Square F Change 13.73533 .22058 1.83878 .0000 Standard Error Signif F Change Dependent Variable.. WORTH Equation Number 1 Beginning Block Number 2. Method: Enter Variable(s) Entered on Step Number OUTGOING OUTGOING 3.. .55210 Multiple R .30482 R Square R Square Change .06692 .28084 Adjusted R Square F Change 8.37421 Standard Error 1.76626 Signif F Change .0048

 Part of LSQREG2.SPS revised

 REGRESSION

 DESCRIPTIVES=MEAN STDDEV CORR N

 /variables = fgood worth angry arrange copertiv outgoing

 /variables = fgood worth angry arrange copertiv outgoing

 /statistics = r coeff anova outs zpp cha

 /DEPENDENT=angry

 /method=enter copertiv outgoing

 /method=enter arrange.

 finish.

 Equation Number 1
 Dependent Variable.
 WORTH

Beginning Block Number 1. Method: Enter COPERTIV OUTGOING Variable(s) Entered on Step Number 1.. OUTGOING 2.. COPERTIV Multiple R .52735 R Square .27810 R Square Change .27810

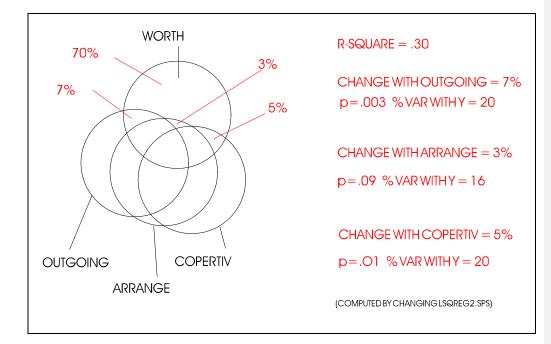
Adjusted R Square Standard Error	.26169 1.78962	F Change Signif F Change	16.95029 .0000
Equation Number 1 Beginning Block Num Variable(s) Entered 3 ARRANGE	ber ² . Method:		GE
Multiple R R Square Adjusted R Square Standard Error	.55210 .30482 .28084 1.76626	R Square Change F Change Signif F Change	.02672 3.34348 .0709

Part of LSQREG2.SPS revised

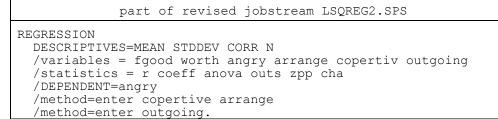
REGRESSION DESCRIPTIVES=MEAN STDDEV CORR N /variables = fgood worth angry arrange copertiv outgoing /statistics = r coeff anova outs zpp cha /DEPENDENT=angry /method=enter arrange outgoing /method=enter copertiv. finish.

Equation Number 1 Dependent Variable.. WORTH Beginning Block Number 1. Method: Enter ARRANGE OUTGOING Variable(s) Entered on Step Number 1.. OUTGOING 2.. ARRANGE .50420 Multiple R .25422 R Square R Square Change .25422 .23727 14.99834 Adjusted R Square F Change Signif F Change Standard Error 1.81899 .0000 Equation Number 1 Dependent Variable.. WORTH Beginning Block Number 2. Method: Enter COPERTIV Variable(s) Entered on Step Number 3.. COPERTIV Multiple R .55210 .30482 .05060 R Square R Square Change Adjusted R Square .28084 F Change 6.33249 1.76626 Standard Error Signif F Change .0137

The above analysis is demonstrated by the following $\ensuremath{\mathsf{Venn}}$ diagrams.



Comment [COMMENT2]: lsqreg1.cdr



finish.

Equation Number 1 Dependent Variable.. ANGRY Beginning Block Number 1. Method: Enter COPERTIV ARRANGE Variable(s) Entered on Step Number COPERTIV 1.. 2.. ARRANGE Multiple R .43846 .19224 .19224 R Square R Square Change Adjusted R Square .17468 F Change 10.94789 Standard Error 1.70038 Signif F Change .0001 Equation Number 1 Dependent Variable.. ANGRY Beginning Block Number 2. Method: Enter OUTGOING Variable(s) Entered on Step Number 3.. OUTGOING Multiple R .48304 .23333 R Square Change R Square .04108 Adjusted R Square .20805 F Change 4.87627 1.66565 Standard Error Signif F Change .0297

part of revised jobstream LSQREG2.SPS

REGRESSION DESCRIPTIVES=MEAN STDDEV CORR N /variables = fgood worth angry arrange copertiv outgoing /statistics = r coeff anova outs zpp cha /DEPENDENT=angry /method=enter copertive outgoing /method=enter arrange. finish.

Equation Number 1 Dependent Variable.. ANGRY Beginning Block Number 1. Method: Enter COPERTIV OUTGOING Variable(s) Entered on Step Number 1.. OUTGOING 2.. COPERTIV Multiple R .44650 .19937 R Square Change .19937 R Square Adjusted R Square .18196 F Change 11.45445 Standard Error 1.69287 Signif F Change .0000

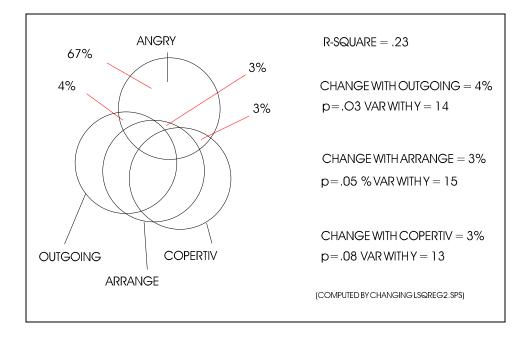
Equation Number 1 Dependent Variable.. ANGRY Beginning Block Number 2. Method: Enter Variable(s) Entered on Step Number ARRANGE 3.. ARRANGE .48304 Multiple R .23333 R Square Change .03396 R Square Adjusted R Square .20805 F Change 4.03094 Standard Error Signif F Change .0476 1.66565

part of revised jobstream LSQREG2.SPS

REGRESSION DESCRIPTIVES=MEAN STDDEV CORR N /variables = fgood worth angry arrange copertiv outgoing /statistics = r coeff anova outs zpp cha /DEPENDENT=angry /method=enter arrange outgoing /method=enter copertiv. finish.

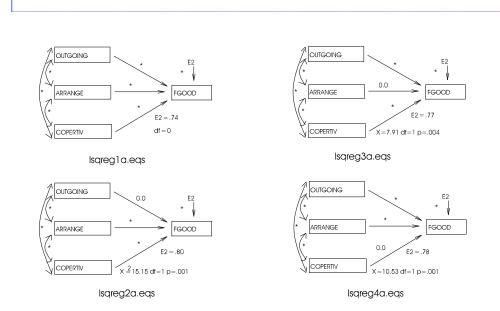
Equation Number 1 Dependent Variable.. ANGRY Beginning Block Number 1. Method: Enter ARRANGE OUTGOING Variable(s) Entered on Step Number 1.. OUTGOING 2.. ARRANGE Multiple R .45520 .20721 R Square R Square Change .20721 Adjusted R Square .18997 F Change 12.02270 Signif F Change Standard Error 1.68456 .0000 Dependent Variable.. Equation Number 1 ANGRY Beginning Block Number 2. Method: Enter Variable(s) Entered on Step Number COPERTIV 3.. COPERTIV .48304 Multiple R R Square .23333 R Square Change .02612 F Change Adjusted R Square .20805 3.10026 Standard Error Signif F Change 1.66565 .0816

The above data is represented by the following Venn diagrams.



The same task can be accomplished using EQS. In order to determine variance accounted for by V11 (OUTGOING) the arrow going from V11 to V1 (FGOOD) is eliminated. The following diagram shows first the model with the arrow free (estimated -- the variance of OUTGOING is assessed when it is estimated), and then again when the arrow is set to 0 or is missing (the results are the same when the arrow is set to 0 or is missing).

Comment [COMMENT3]: lsqregla.cdr



Some hand calculations need to be performed in order to obtain the results found in the multiple regression. In the multiple regression it was found that OUTGOING accounted for 9% unique variance of FGOOD. This result can be obtained in the following manner. In the first run of EQS where all three variables were predicting FGOOD E2 was .74. That number squared in the proportion of error variance (.5476). That is the same as was found in the

multiple regression solution. There is a slight difference because of the different methods of calculation. At any rate when this is subtracted from 1 the result is .4524; the proportion FGOOD variance accounted for by OUTGOING, ARRANGE, and COPERTIV. The amount of unique variance accounted for by OUTGOING is obtained by squaring 80 (80 * 80 = .64), subtracting that result from 1 (1 -.64 = .36), and then subtraction that from the variance accounted for by all three (.4524 - .36 = .0924) indication .09 proportion or 9% variance. Each of the other unique variances can be accounted for in the same manner.

The jobstreams for the four models in the figure are as follows:

LSQREG1A.EQS /TITLE multiple regression model 1 /SPE CASE=97; VAR = 19; ME=ML; DA='lsqcorl.cv1'; /LABELS v3=WORTH; v1=ENJOY: v2=FGOOD; v4=FEARFUL; v5=ANGRY; v10=SUSPICIS; v6=TENSE; v7=SHY; v8=FUN; v9=SORRY; v11=OUTGOING; v12=arrange; v13=copertiv; v14=PEOPLE; v15=INCLUDED; v16=CONFRONT; v17=frsupp; v18=FRLEIS; v19=TTALK; /wtest /lmtest /EQU V2 =*v11 + *v12 + *v13 + e2; /VAR v11=*;v12=*;v13=*; e2 = *; /cov v11,v12=*; v11,v13=*; v12,v13=*; /END

LSQREG2A.EQS				
/TITLE				
multiple regression model 1 /SPE				
CASE=97; VA DA='lsqcor1.c /LABELS v1=ENJOY; v6=TENSE;	<pre>R = 19; ME=ML; v1'; v2=FGOOD; v7=SHY;</pre>	v3=WORTH; v8=FUN;	v4=FEARFUL; v9=SORRY;	v5=ANGRY; v10=SUSPICIS;

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```

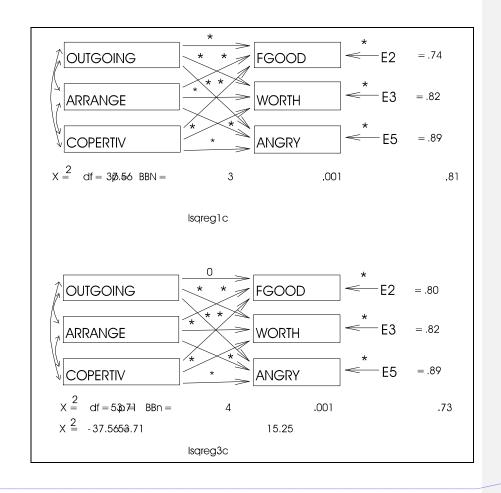
```
v11=OUTGOING; v12=arrange; v13=copertiv; v14=PEOPLE; v15=INCLUDED;
v16=CONFRONT; v17=frsupp; v18=FRLEIS; v19=TTALK;
/wtest
/lmtest
/EQU
v2 =0v11 + *v12 + *v13 + e2;
/VAR
v11=*;v12=*;v13=*;
e2 = *;
/cov
v11,v12=*;
v12,v13=*;
v12,v13=*;
/END
```

LSQREG3A.EQS /TITLE multiple regression model 1 /SPE CASE=97; VAR = 19; ME=ML; DA='lsqcorl.cvl'; /LABELS v2=FGOOD; v3=WORTH; v7=SHY; v8=FUN; v4=FEARFUL; v5=ANGRY; v9=SORRY; v10=SUSPI v1=ENJOY; v6=TENSE; v10=SUSPICIS; v11=OUTGOING; v12=arrange; v13=copertiv; v14=PEOPLE; v15=INCLUDED; v16=CONFRONT; v17=frsupp; v18=FRLEIS; v19=TTALK; /wtest /lmtest /EQU V2 =*v11 + 0v12 + *v13 + e2; /VAR v11=*;v12=*;v13=*; e2 = *; /cov v11,v12=*; v11,v13=*; v12,v13=*; /END

LSQREG4A.EQS
/TITLE
multiple regression model 1 /SPE
CASE=97; VAR = 19; ME=ML;

```
DA='lsqcorl.cv1';
/LABELS
 v1=ENJOY;
               v2=FGOOD;
                             v3=WORTH;
                                            v4=FEARFUL;
                                                          v5=ANGRY;
 v6=TENSE;
               v7=SHY;
                                            v9=SORRY;
                                                          v10=SUSPICIS;
                              v8=FUN;
 v11=OUTGOING; v12=arrange; v13=copertiv; v14=PEOPLE;
                                                          v15=INCLUDED;
                              v18=FRLEIS;
 v16=CONFRONT; v17=frsupp;
                                            v19=TTALK;
/wtest
/lmtest
/EQU
 V2 =*v11 + *v12 + 0v13 + e2;
/VAR
 v11=*;v12=*;v13=*;
  e2 = *;
/cov
 v11,v12=*;
 v11,v13=*;
 v12,v13=*;
/END
```

The problem with using this method is that the difference between each model and the original cannot be assessed because the original has 0 degrees of freedom and consequently, no chi-square. However, the next method solves the problem. Note which path is set to equal 0 in each of the models. In the first model (the comparison model) all paths are free to be estimated (indicated with an "*"). In the next model (labeled "lsqreg3c" in the figure) the path from OUTGOING to FGOOD is set to be 0. Consequently, the variance of FGOOD that was accounted by OUTGOING (beyond ARRANGE and COPERTIV) will not be accounted for in model lsqreg3c. Both the amount of variance accounted and its level of significance can now be determined. The amount of variance accounted for is computed by taking the difference between the error variances of FGOOD for the two models. The error variance for FGOOD in model lsqreg1c was .74, and .80 for lsqreg3c. These numbers were obtained from the Standardized Solution of the EQS output.



Comment [COMMENT4]: LSQREG1C.CDR

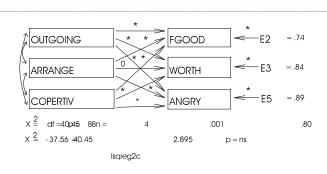
The jobstreams for running the above models are as follows.

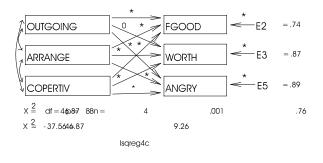
```
LSQREG1C.EQS
/TITLE
 multiple regression model 1
/SPE
CASE=97; VAR = 19; ME=ML;
DA='lsqcor1.cv1';
/LABELS
v1=ENJOY; v2=FGOOD; v3=WORTH; v4=FEARFUL; v5=ANGRY;
v6=TENSE; v7=SHY; v8=FUN; v9=SORRY; v10=SUSPICIS;
 v11=OUTGOING; v12=arrange; v13=copertiv; v14=PEOPLE; v15=INCLUDED;
v16=CONFRONT; v17=frsupp; v18=FRLEIS; v19=TTALK;
/wtest
/lmtest
/EQU
V2 = v11 + v12 + v13 + e2;
v3 = v11 + v12 + v13 + e3;
v5 =*v11 + *v12 + *v13 + e5;
/VAR
v11=*;v12=*;v13=*;
e^{2}, e^{3}, e^{5} = *;
/cov
```

```
v11,v12=*;
v11,v13=*;
v12,v13=*;
/END
```

LSQREG3C.EQS
/TITLE multiple regression model 1 /SPE CASE=97; VAR = 19; ME=ML;
DA='lsqcor1.cv1';
/LABELS
v1=ENJOY; v2=FGOOD; v3=WORTH; v4=FEARFUL; v5=ANGRY; v6=TENSE; v7=SHY; v8=FUN; v9=SORRY; v10=SUSPICIS;
v11=OUTGOING; v12=arrange; v13=copertiv; v14=PEOPLE; v15=INCLUDED;
v16=CONFRONT; v17=frsupp; v18=FRLEIS; v19=TTALK;
/wtest
/lmtest
/EQU
V2 = 0v11 + v12 + v13 + e2;
v3 = v11 + v12 + v13 + e3;
v5 = v11 + v12 + v13 + e5;
/VAR
v11=*;v12=*;v13=*;
e2, e3, e5 = *;
/cov
v11,v12=*;
v11,v13=*;
v12,v13=*;
/END

Comment [COMMENT5]: LSQREG2C.CDR [GEM]





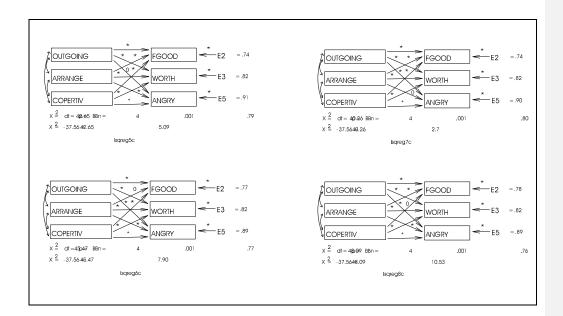
Comment [COMMENT6]: LSQREG2C.CDR [GEM]

LSQREG4C.EQS		
/TITLE multiple regression model 1 /SPE CASE=97; VAR = 19; ME=ML;		
DA='Isqcor1.cv1'; /LABELS		
v1=ENJOY; v2=FGOOD; v3=WORTH; v4=FEARFUL; v5=ANGRY; v6=TENSE; v7=SHY; v8=FUN; v9=SORRY; v10=SUSPICIS;		
v11=OUTGOING; v12=arrange; v13=copertiv; v14=PEOPLE; v15=INCLUDED; v16=CONFRONT; v17=frsupp; v18=FRLEIS; v19=TTALK;		
/wtest		
/Imtest /EQU		
V2 =*v11 + *v12 + *v13 + e2; v3 =0v11 + *v12 + *v13 + e3;		

v5 =*v11 + *v12 + *v13 + e5; /VAR v11=*;v12=*;v13=*; e2, e3, e5 = *; /cov v11,v12=*; v11,v13=*; v12,v13=*; /END

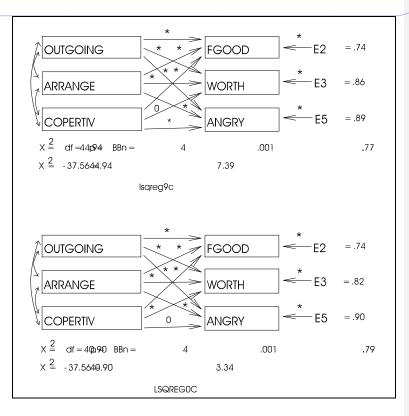
Notice that the only difference between the two jobstreams is the a 0 is added before "V11" in the first line of the equation section in the second jobstream. This next figure shows ____ models.

Comment [COMMENT7]: LSQREG5C.CDR [GEM]



All of the necessary jobstreams for the above or below models are not shown since there would be considerable redundancy.

[enter lsqreg9c.dc2 here]



Comment [COMMENT8]: LSQREG9C.CDR [GEM]

Now we will move to the next level of analysis in parceling variance. Up until now all of the calculations could be accomplished using multiple regression. These next models could not be done using multiple regression. In the first example a factor will be used in place of a single measured variable. It is similar to multiple regression in that there is a number of dependent variables and a single independent (variable), however, in this case the dependent variable is a factor.

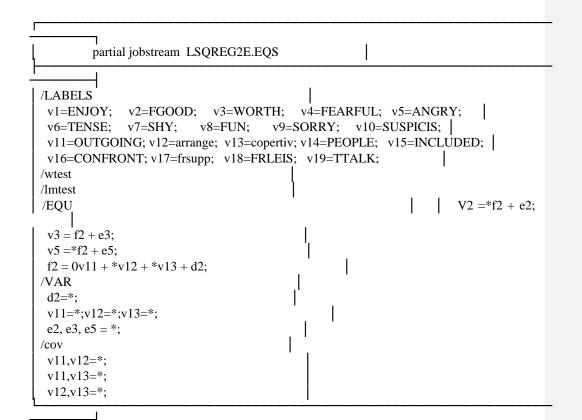
[enter lsqreg1e.dc2 here]

Comment [COMMENT9]: LSQREG1E.CDR [GEM]

The jobstreams for running the above models follow.

partial jobstream LSQREG1E.EQS /LABELS v1=ENJOY; v2=FGOOD; v3=WORTH; v4=FEARFUL; v5=ANGRY; v6=TENSE; v7=SHY; v8=FUN; v9=SORRY; v10=SUSPICIS; v11=OUTGOING; v12=arrange; v13=copertiv; v14=PEOPLE; v15=INCLUDED; v16=CONFRONT; v17=frsupp; v18=FRLEIS; v19=TTALK; /wtest /lmtest /EQU V2 = *f2 + e2;v3 = f2 + e3;v5 = f2 + e5;f2 = *v11 + *v12 + *v13 + d2;/VAR d2=*; v11=*;v12=*;v13=*; e2, e3, e5 = *; /cov v11,v12=*; v11,v13=*; v12,v13=*;

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Two more models are presented without jobstreams.

[enter lsqreg3e.dc2 here]

In the above examples we have been able to assess the variance accounted for in a variable or factor by using the error variance of the dependent variable. This next set of models shows some restrictions in using this method. Particularly, the point is made that in order to parse out variance and use the error variance as the residual, the two models used to show the change must meet the two following restrictions: (1) one model must be nested in the other model (must be the same number of measured and latent variables), (2) the difference between the two models must only be an arrow that points at the variable in question (the one that you are attempting to account for the variance of).

[enter lsqregb.dc2 here]

[enter lsqreg1b.dc2 here]

The FGOOD variable of models "lsqreg1b" cannot be assessed for the variance accounted for by the factor F1, but the models LSQREGB can be assessed for the variance accounted for by the factor (you should note that all models labeled LSQREG1B are identical and all models labeled LSQREG1B are identical).

The rule for the LSQREG1B's is that in attempting to assess variance accounted for you cannot reduce (eliminate) an arrow that estimates from a factor. The arrow that is eliminated must be pointing at the variable that the error variance is being assessed. Only an arrow pointing at a variable will result in being able to test D2. Arrows point away will test that and other things.